

Review IV – Decision Making Under Risk

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Risk Aversion and Expected Utility - 1

1. The expected utility hypothesis was developed by
 - a. Fischer Black and Myron Scholes
 - b. John von Neumann and Oskar Morgenstern
 - c. John Lintner and William Sharpe
 - d. Some Nobel Prize winner.
2. A risk-taking individual will
 - a. Pay less than the expected value for a risky alternative.
 - b. Pay the risky alternative's expected value.
 - c. Pay more than the expected value for a risky alternative.
 - d. It is impossible to determine.

Risk Aversion and Expected Utility - 2

3. The certainty equivalent is
 - a. The expected value of the risky alternative.
 - b. The least dollar amount that a risk averse decision maker will take for the risky alternative.
 - c. The greatest dollar amount that a risk averse decision maker will take for the risky alternative.
 - d. None of the above.
4. The risk premium is
 - a. The most that a risk averse decision maker would pay to remove the risk from a risky alternative.
 - b. The expected benefit from a risky gamble.
 - c. The market price for a risky investment in the capital market.
 - d. None of the above.

Risk Aversion and Expected Utility - 2

- For the next four questions consider a gamble with payoff E_1 of \$ 125,000 and payoff E_2 of \$ 175,000. Also assume that the each outcome is equally likely (i.e., $P[E_1] = P[E_2] = 0.5$). Also assume a power utility function

$$U[Y] = \frac{Y^{(1-r)}}{1-r}. \quad (1)$$

Assume that $r = 1.20$ (Note that the expected utility may be less than zero).

- The expected utility of this alternative is
 - 0.4548
 - 55,250
 - 0.4626
 - None of the above.

Risk Aversion and Expected Utility - 3

6. The certainty equivalent of the risky alternative is
 - a. \$ 110,938
 - b. \$ 147,484
 - c. \$ 160,537
 - d. None of the above
7. The risk premium for this investment is
 - a. \$ 39,063
 - b. \$ 2,516
 - c. \$ 1,963
 - d. None of the above

Risk Aversion and Expected Utility - 4

8. What would happen to the certainty equivalent for $r = 1.20$ if the probability of event 2 ($P[E_2]$) increased and the probability of event 1 ($P[E_1]$) decreased?
- a. The certainty equivalent of the gamble would increase.
 - b. The certainty equivalent of the gamble would decrease.
 - c. The expected value of the gamble would increase.
 - d. a and c.

Portfolio Theory - 1

- For the next three questions use the information in the following table

| Acres Planted in | | | | | Expected | |
|------------------|----------|----------|---------|-------|------------|---------|
| Corn | Cotton | Soybeans | Peanuts | Wheat | Variance | Income |
| 287.89 | 992.11 | 0.00 | 0.00 | 0.00 | 2.441E+10 | 450,000 |
| 212.11 | 1,067.89 | 0.00 | 0.00 | 0.00 | 1.9488E+10 | 425,000 |
| 146.06 | 1,104.79 | 29.14 | 0.00 | 0.00 | 1.5403E+10 | 400,000 |
| 94.85 | 1,082.49 | 102.66 | 0.00 | 0.00 | 1.1938E+10 | 375,000 |
| 43.64 | 1,060.18 | 176.18 | 0.00 | 0.00 | 9.0388E+09 | 350,000 |

9. In general, the results presented in the optimal portfolios indicate that
- It is generally more risky to hold two assets than one.
 - It is generally less risky to hold two assets than one.
 - Soybeans are risky
 - None of the above

Portfolio Theory - 2

10. The results in the forgoing table indicate that the Expected Value–Variance frontier is
 - a. Upward sloping - higher returns can only be acquired at a higher variance (more risk).
 - b. Concave - the rate that additional variance is added for expected return increases as returns increase.
 - c. Both a and b.
 - d. Neither a nor b.
11. The highest risk/return relationship across crops is likely to be
 - a. Corn
 - b. Cotton
 - c. Soybeans
 - d. Impossible to tell

Capital Asset Pricing Model - 1

- For the next six questions use the results of the regression

$$r_{it} = \alpha_i + \beta_i r_{mt} + \epsilon_t \quad (2)$$

where r_{it} is the return for stock i and r_{mt} is the return for the market portfolio (e.g., the S & P 500 stock index).

| Stock | α_i | β_i |
|-------|---------------------|--------------------|
| AMD | -0.0029 (0.0029) | 1.2289 (0.2186) |
| MCD | -0.0006 (0.0012) | 0.6807 (0.1131) |
| MSFT | 0.0016 (0.0012) | 1.4273 (0.0906) |

Capital Asset Pricing Model - 2

12. The Capital Asset Pricing Model suggests that
 - a. Market prices for stock adjust based on the market's evaluation of the riskiness of that stock's returns.
 - b. The riskiness of a stock can be estimated based on how the return on that stock responds to changes in the market portfolio's returns.
 - c. Assumes arbitrage efficiency – buyers must be able to buy and sell the stock at any time – for this valuation to be appropriate.
 - d. All of the above.
13. The riskiest stock in the above analysis is
 - a. AMD
 - b. MCD
 - c. MSFT
 - d. All the stocks are equally risky.

Capital Asset Pricing Model - 3

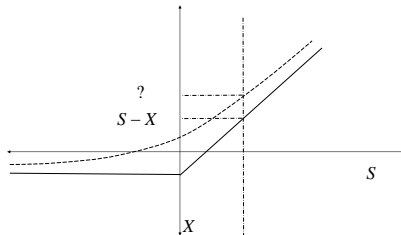
14. Given an expected return on S & P 500 of 0.080 and a risk-free interest rate of 0.028, the risk adjusted rate or return for McDonalds' (MCD) is
- a. 0.0919
 - b. 0.0634
 - c. 0.1022
 - d. None of the above.
15. The fact that the α s are relatively small supports the contention that
- a. The stock market appears to be fairly volatile at the current time.
 - b. The stock market is fairly close to equilibrium (i.e., the returns are largely explained by their relative riskiness).
 - c. We should expect inflation in the near future.
 - d. None of the above.

Black-Scholes Option Pricing Models - 1

16. A call option gives the bearer the right but does not require
- a. is an instrument that gives the bearer the right to purchase a stock at a fixed price over a specified time period.
 - b. is an instrument that gives the bearer the right to sell a stock at a fixed price over a specified time period.
 - c. Both a and b
 - d. Neither a nor b.
17. The Black-Scholes option pricing formula is a function of
- a. Today's stock price and the strike price (the price that the option can be executed at).
 - b. The daily volatility of the stock price.
 - c. The risk-free interest rate.
 - d. All of the above.

Black-Scholes Option Pricing Models - 2

18. The graph below is the payoff function for a
- a. A call option
 - b. A put option
 - c. The Capital Asset Pricing Model
 - d. None of the above.



Stochastic Net Present Value - 1

- Assume that the following table contains 15 draws from a stochastic Net Present Value of an investment with an initial investment of \$ 500 (already included in the Net Present Value values).

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | NPV |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|--------|
| 65.34 | 320.90 | 218.49 | 122.12 | 308.33 | 130.18 | 172.62 | -90.21 | 179.78 | -2.17 | 704.56 |
| -52.43 | 181.71 | 105.80 | 26.43 | 18.65 | 119.76 | 14.36 | 1.84 | 123.49 | -61.14 | -98.06 |
| 339.81 | 54.20 | -12.49 | 172.03 | -112.87 | -21.26 | 50.97 | 264.62 | 426.00 | 76.25 | 737.25 |
| -5.02 | 189.35 | -61.33 | 220.82 | 223.73 | 47.84 | 155.82 | 183.96 | 146.19 | 196.51 | 514.46 |
| 32.49 | 154.83 | -89.51 | 40.80 | 279.16 | -172.63 | 82.29 | 340.98 | 77.08 | 272.09 | 272.36 |
| -257.79 | 210.92 | 273.98 | 163.92 | -74.93 | 211.55 | -44.42 | 102.52 | 298.00 | -58.59 | 147.37 |
| -73.62 | -37.36 | 164.24 | 151.73 | -3.54 | -163.21 | 37.35 | 210.17 | 207.34 | 83.06 | -77.77 |
| -17.51 | -46.54 | -185.34 | 268.33 | 237.58 | 12.53 | 333.95 | 249.73 | -64.80 | -49.58 | 67.14 |
| 184.92 | 57.98 | 321.50 | 6.83 | 166.77 | 21.74 | 250.92 | 29.80 | 46.52 | 67.20 | 467.85 |
| 213.64 | 260.95 | -188.83 | 268.69 | 206.20 | 20.63 | -101.51 | 183.23 | -4.87 | 189.08 | 375.34 |
| -98.18 | 57.32 | -178.44 | 142.81 | 111.16 | 139.94 | -67.48 | 54.39 | 279.13 | 166.13 | -79.19 |
| -106.72 | 61.58 | 163.63 | 135.35 | 37.78 | 137.70 | 338.03 | 222.61 | 212.56 | 85.23 | 481.83 |
| -0.42 | -120.25 | -136.28 | -164.13 | 166.39 | 74.65 | 471.44 | 215.52 | 299.37 | 304.23 | 254.32 |
| 222.15 | 306.43 | 95.02 | 187.60 | -43.60 | 334.06 | 202.96 | 155.99 | -113.48 | -119.03 | 578.00 |
| 164.14 | 223.25 | 40.61 | -130.25 | 526.31 | 126.26 | 264.23 | -156.77 | 159.87 | 170.37 | 635.03 |
| 40.72 | 125.02 | 35.40 | 107.54 | 136.48 | 67.98 | 144.10 | 131.23 | 151.48 | 87.98 | 332.03 |
| 157.67 | 133.39 | 172.24 | 129.31 | 171.03 | 130.55 | 167.42 | 138.71 | 146.75 | 128.11 | 288.74 |

Stochastic Net Present Value - 1

19. Assuming a negative exponential utility function

$$U(\mu, \sigma^2) = \mu - \frac{\rho}{2}\sigma^2 \quad (3)$$

and a risk aversion coefficient $\rho = 0.003$ would you make this investment?

20. What is the probability that the investment will not be able to make its required cash flow in Year 6?